

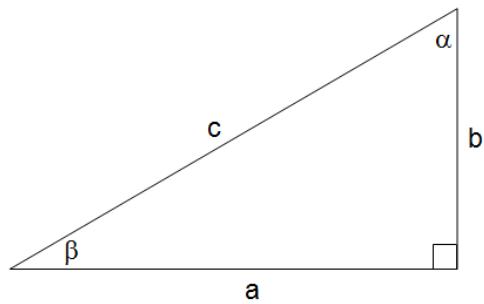
TAREA 2 Unidad 2.

En los problemas del 23-27, calcular las incógnitas indicadas.

Cada problema se refiere al mismo triángulo.

23. $a = 4$, $\beta = 27^\circ$; $b = ?$, $c = ?$

$$\begin{aligned}\tan 27^\circ &= \frac{b}{a} & c^2 &= a^2 + b^2 \\ \tan 27^\circ &= \frac{b}{4} & c^2 &= (4)^2 + (2.03)^2 \\ b &= \tan 27^\circ (4) & c^2 &= 16 + 4.12 \\ b &= 2.03 & c &= \sqrt{20.153} \\ & & c &= 4.489\end{aligned}$$



24. $a = 4$, $b = 10$; $c = ?$, $\beta = ?$, $a = ?$

$$\begin{aligned}\tan \beta &= \frac{b}{a} & c^2 &= a^2 + b^2 \\ \tan \beta &= \frac{10}{4} & c^2 &= (4)^2 + (10)^2 \\ \beta &= \tan^{-1}(\frac{10}{4}) & c^2 &= 16 + 100 \\ \beta &= 68.19^\circ & c^2 &= 116 \\ & & c &= \sqrt{116} \\ & & c &= 10.77\end{aligned}$$

$$\begin{aligned}\alpha &= 180^\circ - 90^\circ - \beta^\circ \\ \alpha &= 180^\circ - 90^\circ - 68.19^\circ \\ \alpha &= 21.81^\circ\end{aligned}$$

25. $b = 8$, $\beta = 34.33^\circ$; $a = ?$, $c = ?$

$$\begin{aligned}\tan \beta &= \frac{b}{a} & \sin \beta &= \frac{b}{c} \\ \tan 34.33^\circ &= \frac{8}{a} & \sin 34.33^\circ &= \frac{8}{c} \\ a(\tan 34.33^\circ) &= 8 & c(\sin 34.33^\circ) &= 8 \\ a &= \frac{8}{\tan 34.33} & c &= \frac{8}{\sin 34.33} \\ a &= 11.71 & c &= 14.18\end{aligned}$$

26. $a = 9$, $c = 12$; $\beta = ?$, $\alpha = ?$, $b = ?$

$$\begin{aligned}\cos \beta &= \frac{a}{c} & c^2 &= a^2 + b^2 \\ \beta &= \cos^{-1}(\frac{9}{12}) & b^2 &= a^2 - c^2 \\ \beta &= 41.40^\circ & b^2 &= 144 - 81 \\ & & b^2 &= 63 \\ \alpha &= 90^\circ - \beta^\circ & b &= \sqrt{63} \\ \alpha &= 90^\circ - 41.40^\circ & b &= 7.93 \\ \alpha &= 48.60^\circ\end{aligned}$$

27. $b = 1.5$, $c = 3$; $\beta = ?$, $\alpha = ?$, $a = ?$

$$\begin{aligned}\sin \beta &= \frac{b}{c} & c^2 &= a^2 + b^2 \\ \beta &= \sin^{-1}(\frac{1.5}{3}) & a^2 &= b^2 - c^2 \\ \beta &= \sin^{-1}(\frac{1.5}{3}) & a^2 &= (3)^2 - (1.5)^2 \\ \beta &= 30^\circ & a^2 &= 9 - 2.25 \\ & & a^2 &= 6.75 \\ \alpha &= 90^\circ - \beta^\circ & a &= \sqrt{6.75} \\ \alpha &= 90^\circ - 30^\circ & a &= 2.598 \\ \alpha &= 60^\circ\end{aligned}$$